





Lecture 2

- Surd Expressions
- Perfect Square Trinomials
- Theorem of Pythagoras
- Rationalizing the denominator
- Factorization of zero
- Inequalities



 $(a+bi)(a-bi) = a^2 - aki + bia - b^2i^2$

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Surd Expressions



- Any expression involving a square root symbol $\sqrt{}$
- When we can't simplify a number to remove a square root (or cube root etc.) then it is **a surd**.
- The surds have a decimal which goes on forever without repeating, and are <u>Irrational Numbers</u>.

•
$$\sqrt{2}, \sqrt{3} + 1, \frac{\sqrt{13-a}}{\sqrt{b+c}}, \dots$$
 - surd expressions

- $\sqrt{a} \rightarrow a \ge 0$
- - \sqrt{a} is possible
- $\sqrt{-a}$ is an imaginary number

Squares and Differences of Squares

•
$$(a+b)^2 = a^2 + 2ab + b^2$$

•
$$(a-b)^2 = a^2 - 2ab + b^2$$



• $a^2 - b^2 = (a + b)(a - b)$

 $(a+b)^2 = a^2 + 2ab + b^2$

• $(2x^2 + 5)^2 = (2x^2)^2 + 2 \times (2x^2) \times (5) + 5^2 = 4x^4 + 20x^2 + 25$

 $(a-b)^2 = a^2 - 2ab + b^2$ 5730 $(3y^2 - 7)^2 = (3y^2)^2 - 2 \times (3y^2) \times (7) + 7^2 = 9y^4 - 42y^2 + 49$ flags= ft gt. at x = 2.05 ys1 1 Z 3 + 5 ubsorbindication

 $a^2 - b^2 = (a + b)(a - b)$

•
$$4z^2 - 81 = (2z + 9)(2z - 9)$$

 $2z \times 2z \qquad 9 \times 9$
 $a = 2z \qquad b = 9$

•
$$54x^2 - 6y^2 = 6(3x + y)(3x - y)$$

Factor Perfect Square Trinomials

Quick

Recap



 $a^{2} - 2ab + b^{2} = (a - b)(a - b) = (a - b)^{2}$ Take note of the signs

Match Column A with its factor in Column B by joining its line.



Complete the following expression to make a perfect square trinomial.

1) $a^2 + 8a +$ _____ 2) $a^2 - 10a +$ _____ 3) $a^2 + 4a +$ _____ 4) $a^2 - 24a +$ _____ 5) $a^2 - 4a +$ _____ 6) a² + 24a + _____ 7) a² + 12a + _____ 8) a² - 12a + _____ 9) a² - 6a + _____ 10) a² + 10a + _____

Practice

- ♦ $64n^2 32n + 4$
- $10 140n + 490n^2$
- $9 + 18p + 9p^2$
- $x^3y 4xy^3$
- ♦ $288b^2 + 672b + 392$
- $96v^2 + 48v + 6$
- ♦ $640v^2 + 1120v + 490$

- * $49x^2 + 84x + 36$ * $25x^2 + 9$
- * $2y^5 162y$
 - $x^{2} 12x + 4$
 - $31x^2 180x + 100$
 - $36x^2 + 132x + 121$







 $80p^2 + 200p + 125$ $100p^2 - 40p + 4$ $m^2 + 10m + 25$ $2x^2 - 16x + 32$ $125x^2 - 200x + 80$ $16n^2 - 24n + 9$ $16x^2 - 40x + 25$ $4b^2 + 20b + 25$ $9k^2 + 6k + 1$ $27x^2 + 18x + 3$ $100n^2 - 80n + 16$ $4x^2 - 8x + 4$

Theorem of Pythagoras



Practice

Adam is on his way home from work. He drives 35 miles due North and then 42 miles due West. Find the shortest distance he can cover to reach home early.

Rachel bought a rug for her apartment. The rug is 11 feet long and 9 feet wide. Find the diagonal length of the rug.

A 15 feet tree casts a shadow that is 8 feet long. What is the distance from the tip of the tree to the tip of its shadow?







1. Ms. Green tells you that a right triangle has a hypotenuse of 13 and a leg of 5. She asks you to find the other leg of the triangle. What is your answer?

2. Two joggers run 8 miles north and then 5 miles west. What is the shortest distance, to the *nearest tenth* of a mile, they must travel to return to their starting point?

3. Oscar's dog house is shaped like a tent. The slanted sides are both 5 feet long and the bottom of the house is 6 feet across. What is the height of his dog house, in feet, at its tallest point?

4. To get from point A to point B you must avoid walking through a pond. To avoid the pond, you must walk 34 meters south and 41 meters east. To the *nearest meter*, how many meters would be saved if it were possible to walk through the pond?





Rationalizing the denominator

•
$$\frac{1}{a\pm\sqrt{b}} = \left(\frac{1}{a\pm\sqrt{b}}\right) \left(\frac{a\mp\sqrt{b}}{a\mp\sqrt{b}}\right) = \frac{a\mp\sqrt{b}}{a^2-b}$$

$$\frac{\sqrt{3}-1}{\sqrt{3}+1} = \frac{(\sqrt{3}-1)_{x}}{(\sqrt{3}+1)} \frac{(\sqrt{3}-1)}{(\sqrt{3}-1)} = \frac{(\sqrt{3}-1)^{2}}{(\sqrt{3})^{2}-(1)^{2}}$$
$$= \frac{3+1-2\sqrt{3}}{3-1} = \frac{4-2\sqrt{3}}{2} = 2-\sqrt{3}$$
$$a^{2}-b^{2} = (a+b)(a-b)$$

Practice



Factorization of Zero

$$(x-1)(x+3) = 0$$

 \swarrow \searrow
 $x-1 = 0$ $x+3 = 0$
 $x = 1$ $x = -3$

Practice



- (2x+1)(3x-4) $(-\frac{2}{5}x+1)(4x+4)$
- $3(\frac{4x}{5} \frac{1}{7})(1\frac{1}{3} \frac{3x}{10})$ $9(\frac{x}{11} 2\frac{2}{5})(\frac{2}{3} \frac{3x}{12})$

• $(2\sqrt{3}y - 4)(4y + 7)$ • $(9\sqrt{5}z - 13)(24z + 43)$

•
$$(7 - 3\sqrt{5}y)(3y + \frac{2}{3})(\frac{15y}{17} + \frac{34}{55})$$

Inequalities





Inequalities





Practice

If 5 times a number is increased by 4, the result is at least 19. Find the least possible number that satisfies these conditions.

The sum of twice a number and 5 is at most 15. What are the possible values for the number?

Three times a number increased by 8 is no more than the number decreased by 4. Find the number.

The cost of a gallon of orange juice is \$3.50. What is the maximum number of containers you can buy for \$15?

Question 7: Find the smallest integer that satisfies each inequality below.

(a) $2x - 5 \ge 12$ (b) 4x > 9(c) $\frac{x+9}{3} \ge 7$ (d) 7x + 1 > 60(e) $10x - 16 \ge 76$ (f) 9x + 4 > 7x + 15

Question 8: Solve each of the inequalities below

- (a) 6 < x + 3 < 10 (b) $4 \le 2x \le 7$ (c) $1 \le 3x < 9$
- (d) $4 < \frac{x}{5} < 6$ (e) $9 \le 2x + 3 \le 25$ (f) $-3 \le \frac{x}{4} 1 < 0$

Question 9: Find the integers that satisfy each of the inequalities below

- (a) 5 < x < 9 (b) $-3 < x \le 1$ (c) $4 \le 2x \le 8$
- (d) $16 \le 5x + 1 < 31$ (e) $0 \le \frac{x-6}{2} < 2$ (f) $-9 < \frac{x}{4} 1 < -8$

Practice Time

21 1 22 23

Perfect Square Trinomials & Difference of two squares

		1
\succ (4m ³ + n ³)(4m ³ − n ³)	$\blacktriangleright 18z^2 - 96z + 128$	$> 2k^2 - 32km + 128m^2$
\rightarrow 144 x^2 + 264 x + 121	▶ $45a^2 - 240ay + 320y^2$	$> 9x^4 - 4$
(3x+1)(3x-1)	\succ 5(5m ² + 2n ²)(5m ² − 2n ²)	▶ $121n^2 - 110n + 25$
$▶ 36m^2 - 121$	$\succ x^2 - 9y^2$	▶ $50k^2 - 160k + 128$
\succ 6(7r + 5)(7r - 5)	$> 36v^2 - 132v + 121$	\succ 6(2 <i>x</i> + 3)(2 <i>x</i> − 3)
$> x^2 + 18x + 81$	$(3x+2)^2$	$\succ -x^2 + 16$
$> 36x^2 + 132x + 121$	$\succ 4a^2 - 81b^2$	$(5p+3)^2$
$(2y+5)^2$	$> 12x^2 - 75$	\succ (8 <i>y</i> − 2) ²
$(5x^2 - 9)^2$	$\succ a^2b - b^3$	$(4z^2 + 8)^2$

Pythagorean theorem

- To wash a window that is 8 metres off the ground, Aisha leans \triangleright a 10 metre ladder against the side of the building. To reach the window, how far from the building should Aisha place the base of the ladder?
- \geq A 9m ladder is placed against a wall. The foot of the ladder is 1.5m from the foot of the wall. How far up the wall does the ladder reach?
- \geq A rectangle is 20cm long and 8cm wide. Find the length of the diagonal of the rectangle.

9m

1.5m

Rationalising the Denominator & Factorization of Zero

$$\begin{array}{c} \searrow \quad \frac{33}{4 - \sqrt{5}} \qquad & \searrow \quad \frac{\sqrt{5} - 7}{\sqrt{5} + 1} \qquad & \searrow \quad \frac{20 - \sqrt{50}}{3\sqrt{2} - 5} \qquad & \searrow \quad \frac{\sqrt{2} + 5}{\sqrt{3} - \sqrt{5}} \\ & \searrow \quad \frac{17\sqrt{3} + 5\sqrt{5}}{2\sqrt{3} - \sqrt{5}} \qquad & \searrow \quad \frac{3\sqrt{x}}{2\sqrt{x} + \sqrt{y}} \qquad & \searrow \quad \frac{\sqrt{7}}{\sqrt{45}} \qquad & \searrow \quad \frac{8}{3\sqrt{x}} \\ \end{array}$$

- > $x(x+2)(x-2)(3x^2-4)$
- $\succ 4(\frac{3y}{12}+2\frac{3}{7})(\frac{5}{9}-\frac{3y}{15})$

 \succ (6 $\sqrt{3}x - 18$)(16x + 70)

> x(2x-1)(x-1)(x+1)

► $(13 - 2\sqrt{8}y)(5y + \frac{6}{13})(\frac{14y}{23} - \frac{46}{77})$

Inequalities

> $8\frac{1}{2} - x < x + 4\frac{5}{6}$	$ -3\frac{2}{9}n + 1\frac{1}{2} < -2\frac{13}{18} + n $	$a + 1\frac{7}{10} > 2a - 1\frac{1}{20}$
$\blacktriangleright 9 \le 2x + 3 \le 25$	\succ 4x + 8 < 32	
$\blacktriangleright \frac{x+3}{2} \ge 5$	$► 9-2x \ge -7x-4x$	$\blacktriangleright 0 \leq \frac{x-6}{2} < 2$
→ 4(x + 1) < 2x + 3	$\triangleright \frac{x+3}{2} \ge 5$	$\succ \frac{x-5}{4} > 2$
$\blacktriangleright 2(2x-9) \geq 22$	► $1 - \frac{3}{2}x \ge x - 4$	> $-9 - \frac{x}{2} ≥ \frac{x}{2} + 1$
$\blacktriangleright \frac{x}{2} + 1 \le 5$	▶ $13x - 12 < 3x + 13$	▶ $6(x+2) < 42$
$-6 + 1\frac{4}{5}x \le -1\frac{1}{3}x + 1\frac{4}{5}x$	$r + 1\frac{5}{8} \le -1\frac{3}{4}r - 1\frac{1}{8}$	$ n - \frac{31}{9} - 9\frac{3}{10} + 13\frac{89}{180} \le 2n + 1\frac{3}{2}$

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Why must we read?

Reading is good for you because it **improves** your **focus**, **memory**, **empathy**, and **communication skills**. It can <u>reduce stress</u>, <u>improve your mental</u> health, and help you <u>live longer</u>. Reading also allows you to learn new things to <u>help you succeed</u> in your *work* and *relationships*.

