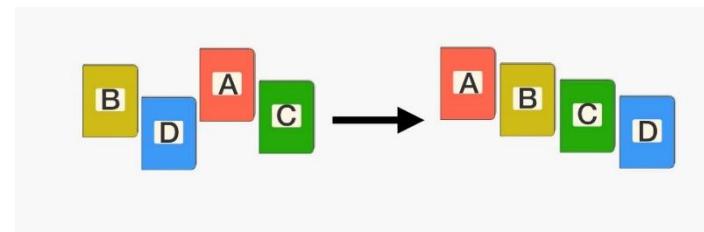
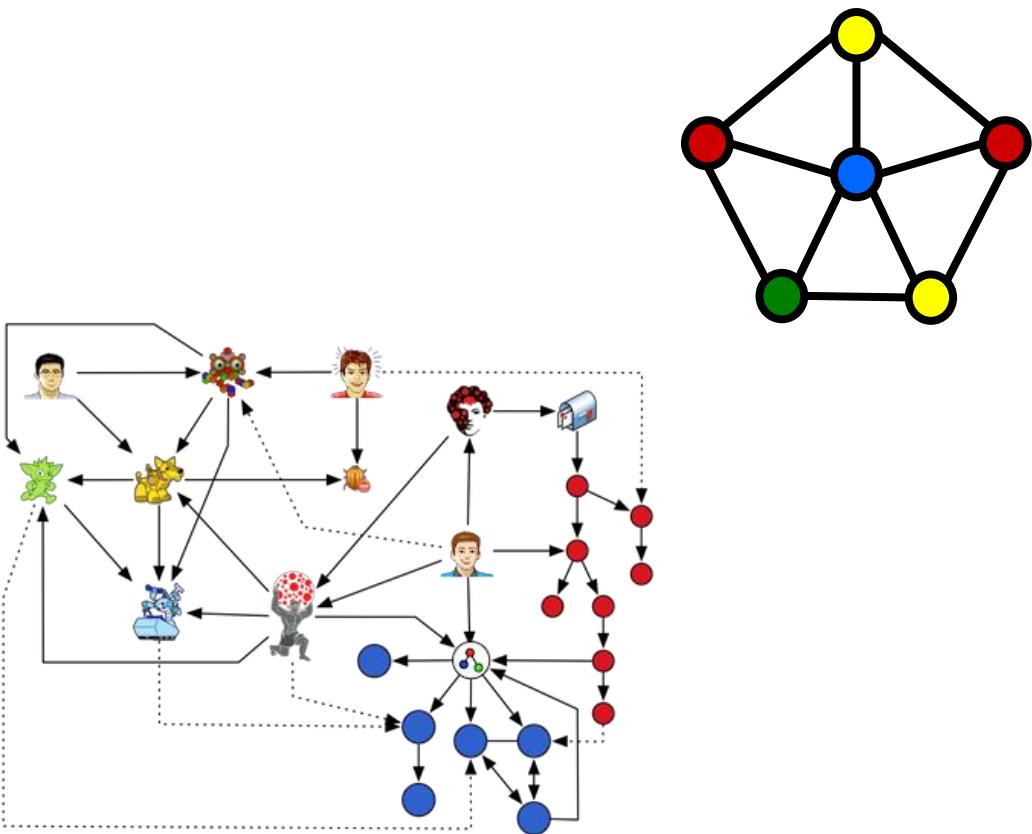




Introduction to Discrete Mathematics



Dr. Salisu Ibrahim
Course Code: IT 235/A/B
Semester 1
Week 1
Date: 04.10.2025



Basic Information



- **Instructor:** Dr. Salisu Ibrahim
- **Lectures:** 3 hours a week
- **Homework:**
 - Will be posted on the SIS system
- **Lecture Notes:**
 - Will be posted on the Lecture Notes web page
- **Office Hours:** Will be announced soon
- **Contact:** via email Salisu.ibrahim@tiu.edu.iq



Course Materials

- Discrete Mathematics and its Applications, 8th edition by Kenneth H. Rosen
- Discrete Mathematics and its Applications, 8th edition by Richard Johnsonbaugh
- Discrete Mathematics with Applications, 5th edition by Susanna S. Epp
- Study links and references for specific topics will be given within Lecture Notes.





Class Regulations

Students have an obligation to arrive on time and remain in the classroom for the duration of scheduled classes and activities.

If students miss more than 10 minutes of any class period or leave before the instructor dismisses the class, they will be marked absent for the whole hour.

Students have an obligation to write, homework, quizzes and final examinations at the times scheduled by the teacher and university.

Students have an obligation to show respectful behavior and appropriate classroom deportment. Should a student be disruptive and/or disrespectful, the teacher has the right to exclude the disruptive student from learning activities (classes) and may refer the case to the Director of Student Services under the Student Code of Conduct.

Mobile Phones are not allowed in the classroom.

Should a student have an emergency case during lecture hours, he/she must raise his hand, and only after lecturer's permission can leave the class.



A Grading Scheme

- Participation/Discussion: **10% (not attendance)**
- Homework: **10%**
- Quizzes: **20% (30% - for exempted students)**
- Midterm: **20%**
- Final Exam **40%**



What is discrete math?

- Discrete math is the study of countable, distinct elements rather than continuous ones.

So instead of smooth-running real numbers, you'll study:

integers

graphs

statements

- Discrete math principles are commonly used in **building algorithms for computer science and data science.**

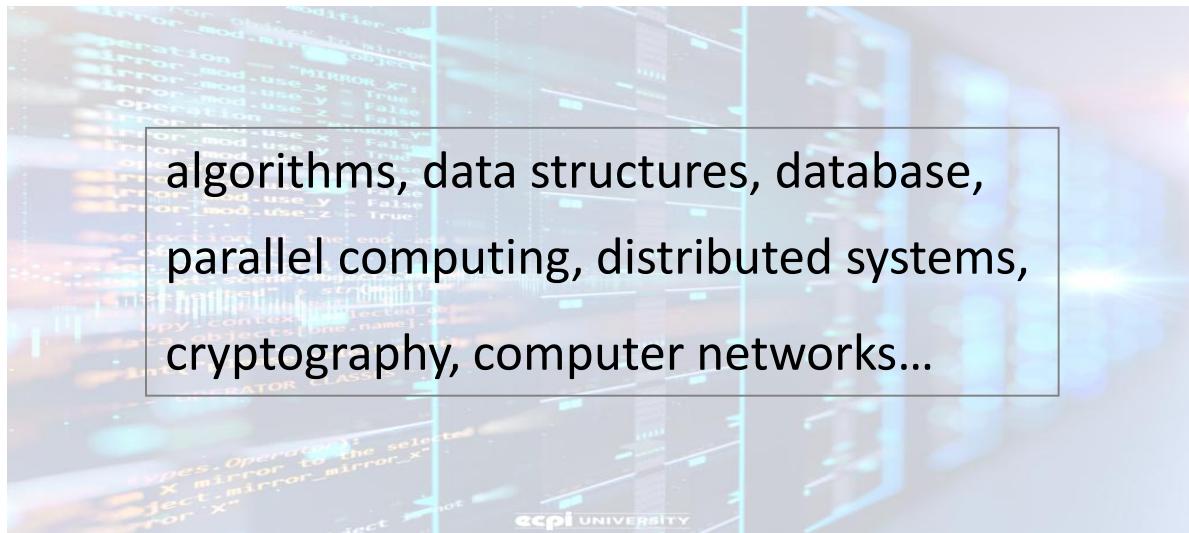




Why Discrete Mathematics?

Design efficient computer systems.

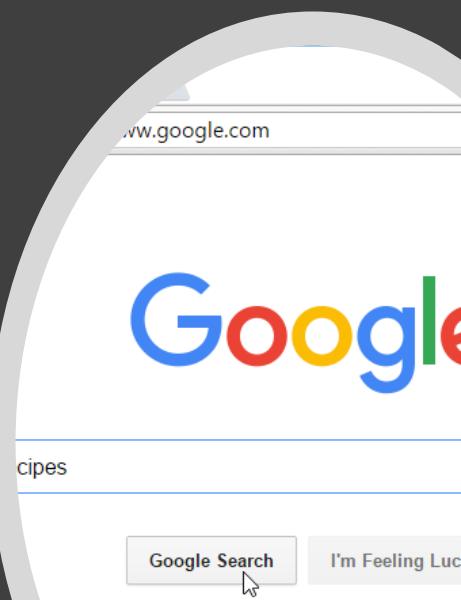
- How did Google manage to build a fast search engine?
- What is the foundation of internet security?

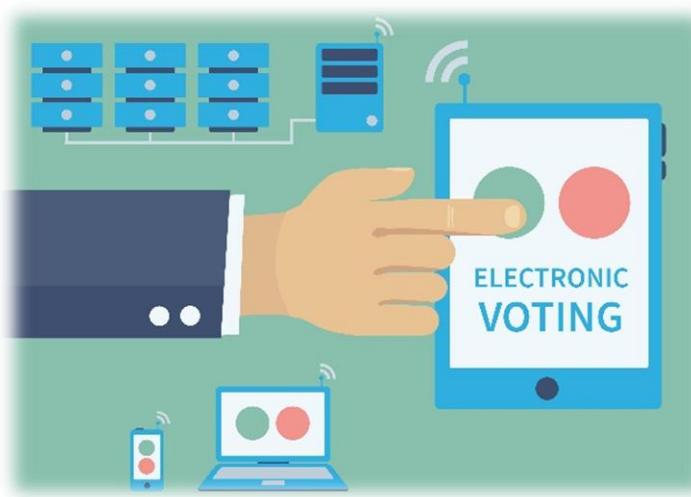


Logic, number theory, counting, graph theory...

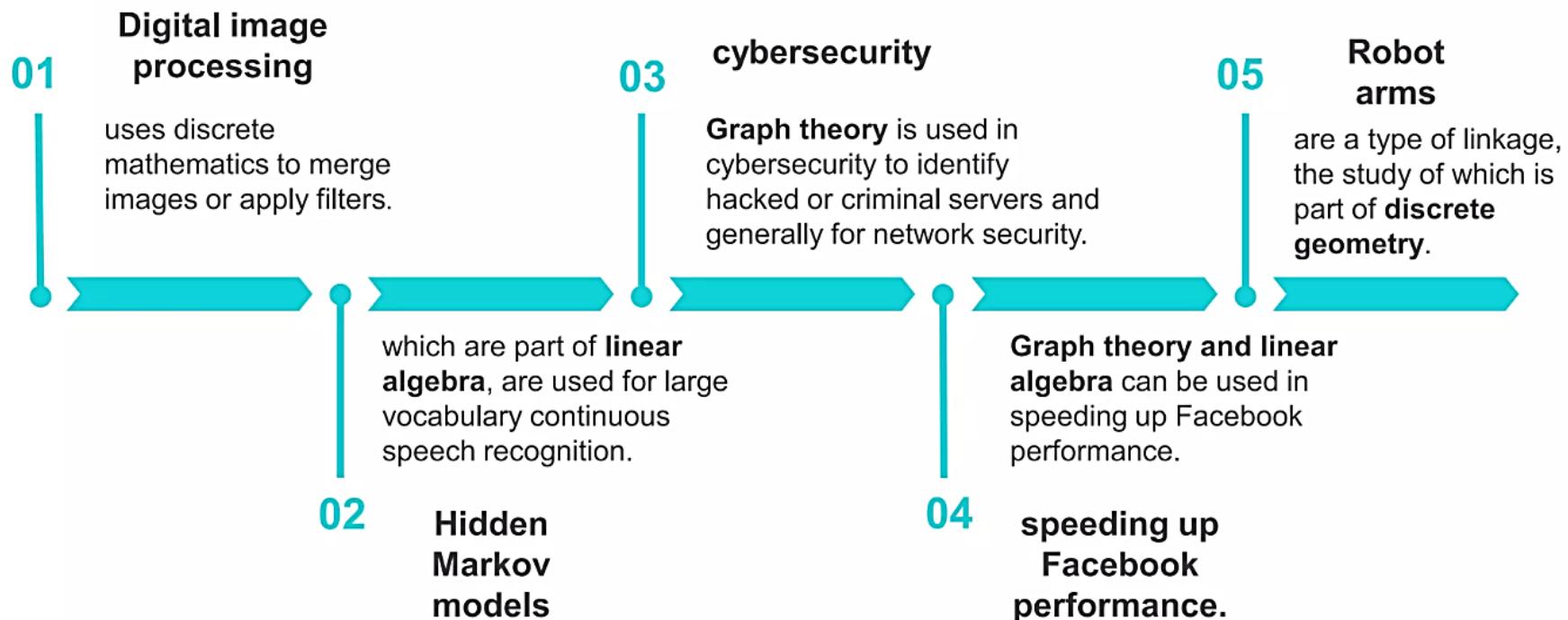


Applications





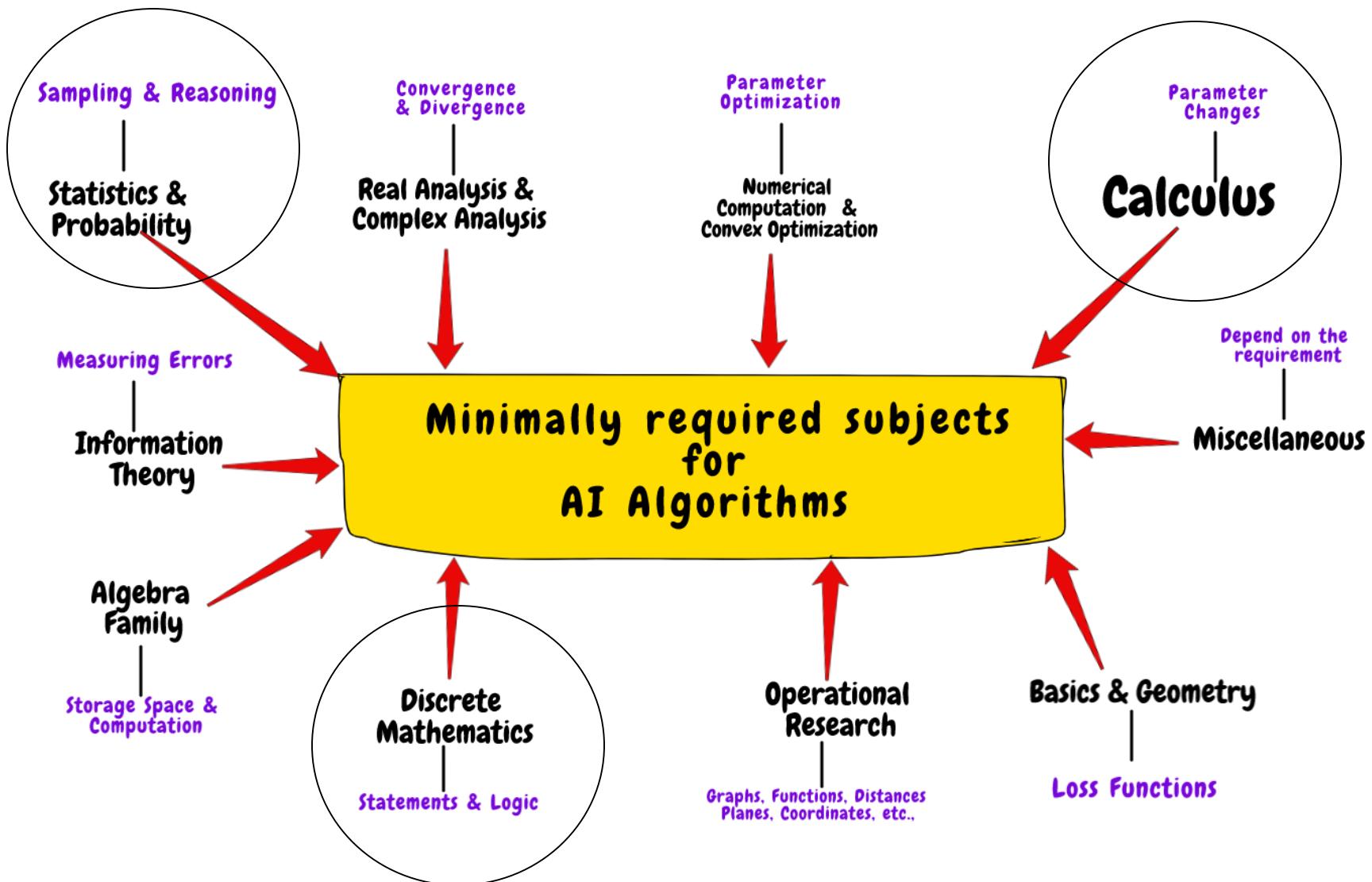
- Computer Graphics (e.g., video games)
- Cryptography (security)
- Networks (“following” on Twitter, “friending” on Facebook, etc.)
- Voting systems
- Logistics
- A programmer uses DM to design efficient algorithms.
- Web Search
- Database
- Scheduling
- Cell phone Communications
- Web Designing



AI

```
V33 - PROCEED - USE THIS STAR FOR MARKS
# COAS CALIBRATION CODE - NO GOOD HERE
# SEE IF ADIMARK BUSY
# BIT2 RESET IN ENDMARK
# STORE VAC ADR IN LOW 9 OF MARKSTAR
# ZERO BITS10 TO 15 RETAINING MKVAC ADR
# SEE IF MARK PART COMPLETE
# SET MKDEX ZERO TO COMPUTE LOS
# LAST PAIR COMPLETE - TO COMPUTE LOS
# NO PAIR BROWNING - SEE IF PAIR-IN-HOT
# NO PAIR ALARM
# MKDEX WAS INITIALIZED ZERO IN MARKCHEX
# IN IT MARK CODE IN COUSPOT FOR TGT*NSM
# THE MARK CODES IN COUSPOT FOR TGT*NSM
# TRAINING ADIMARK - ALLOW EXT VERS
# DISPLAY DEFENT AND STAR CODE
# AND SET IF CODE 1 TO 6
# MARK SYSTEM BUSY - DO ALARM
# YES - ABORT
# NONE AVAILABLE
# PICK UP VAC AREA ADR
# INHIBIT VAC ADR IN XYMARK FOR AYSTAR
# STAY VAC COMPLETE - TO COMPUTE LOS
# NO PAIR BROWNING - SEE IF PAIR-IN-HOT
# NO PAIR ALARM
# MKDEX WAS INITIALIZED ZERO IN MARKCHEX
# IN IT MARK CODES IN COUSPOT FOR TGT*NSM
```

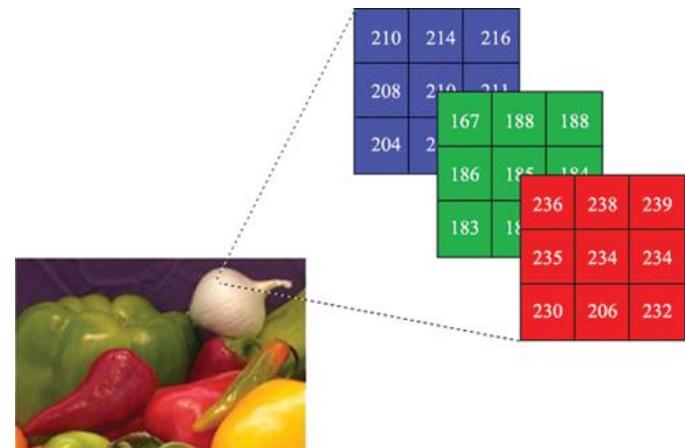
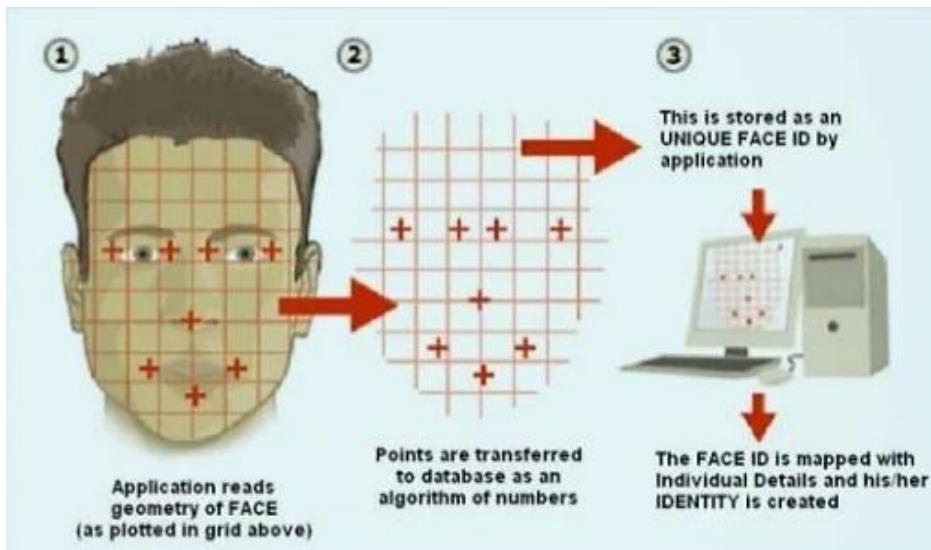




Digital Image Processing

In computer science, digital image processing is the use of computer algorithms to perform image processing on digital images to get an enhanced image or to extract some useful information from it.

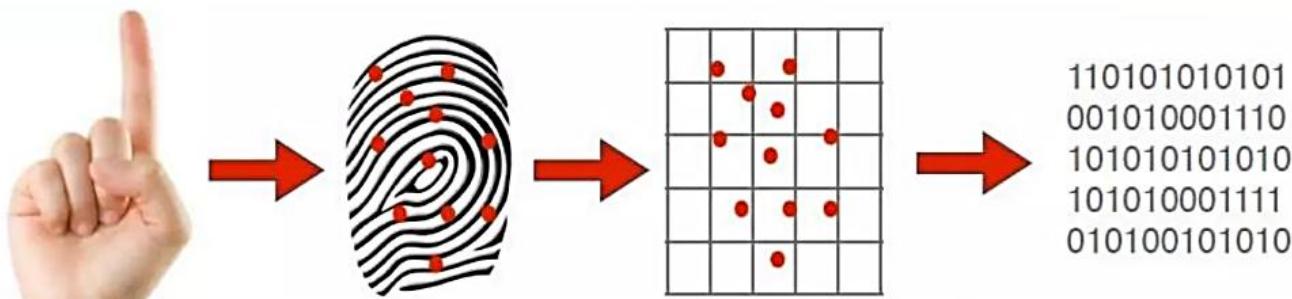
It allows a much wider range of algorithms to be applied to the input data and can avoid problems such as the build-up of noise and signal distortion during processing.



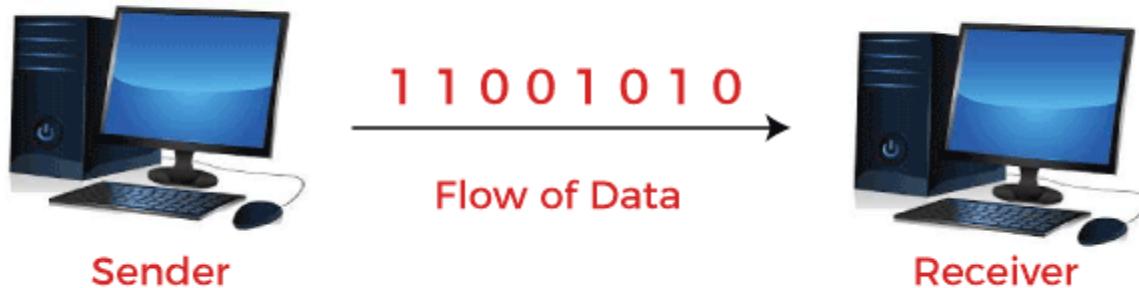
Fingerprint Optical Scanner

Fingerprint Optical Scanner measures your finger electrically.

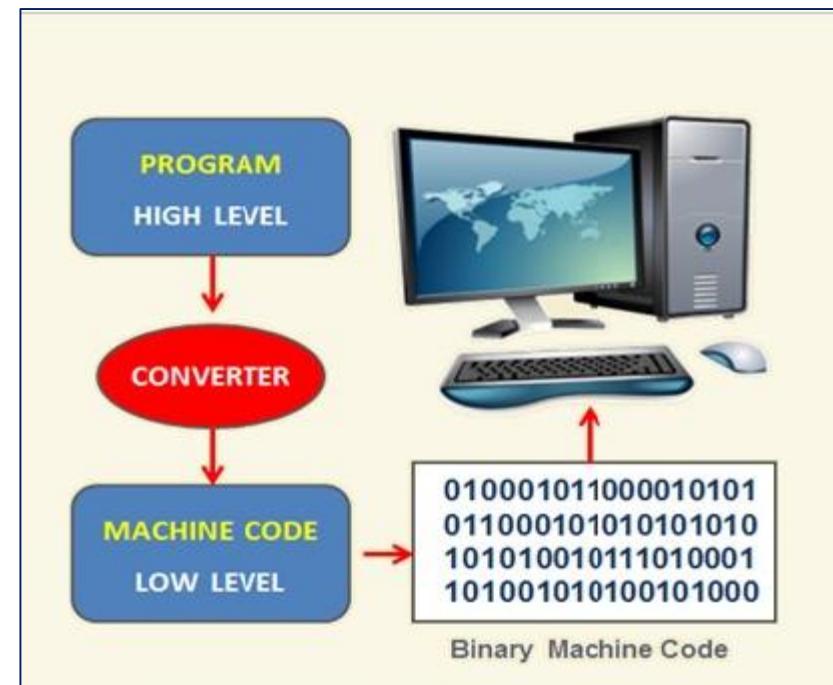
Only specific characteristics, which are unique to every fingerprint, are filtered and saved as an encrypted biometric key or mathematical representation. No image of a fingerprint is ever saved, only a series of numbers (a binary code), which is used for verification. The algorithm cannot be reconverted to an image, so no one can duplicate your fingerprints.



Serial Communication



Run software and store files. The software and files are both stored as huge strings of 1s and 0s. Binary math is discrete mathematics.





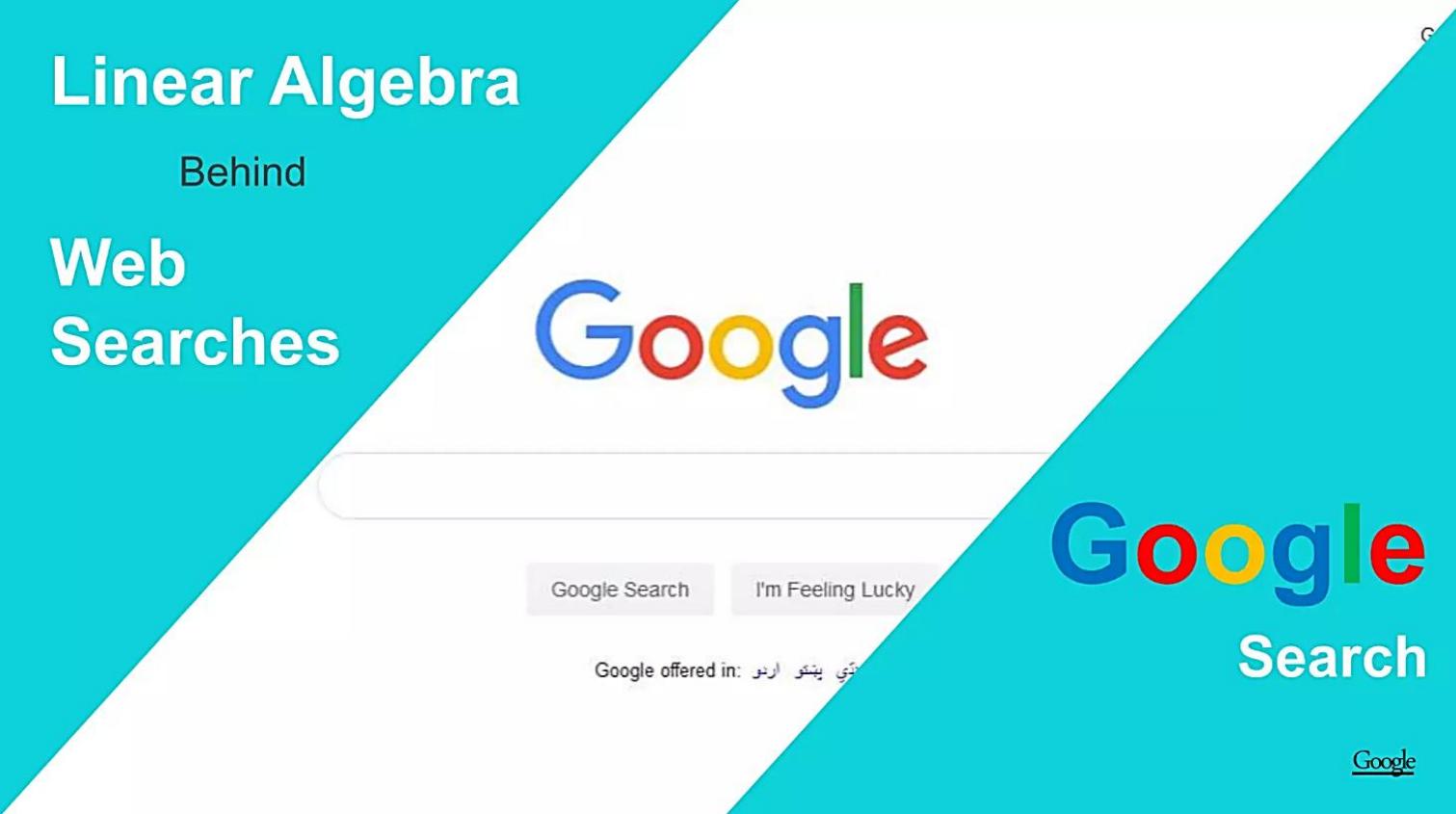
Google Maps

- Uses discrete mathematics to determine fastest driving routes and times.
- Google Maps knows your position via the Global Positioning System.
- Edsger W. Dijkstra's Algorithm is used to calculate shortest route.
- Co-ordinate geometry is used.

Linear Algebra

Behind

Web Searches



A screenshot of the Google search homepage is shown, featuring the iconic Google logo at the top. Below the logo is a search bar with a magnifying glass icon. Underneath the search bar are two buttons: "Google Search" and "I'm Feeling Lucky". At the bottom of the page, the text "Google offered in: " is followed by a list of languages including English, French, German, and Spanish. The entire image is partially covered by a large, solid teal diagonal shape that starts from the top-left and extends to the bottom-right. In the bottom right corner of this teal area, the word "Search" is written in white. The overall background of the slide is white.

Google

Google
Search

[Google](#)

Magic Behind Google Success



When Google went online in 1990's, one thing that set it apart from other search engines was its search result listings which always delivered "good stuff".

Search Engines like Google have to do three basic things :

01

Look the web and locate all web pages with public access.

02

Indexing of searched data for more efficient search.

03

Rate the importance of each page in the database, so when the user does a search, the more important pages are presented first.

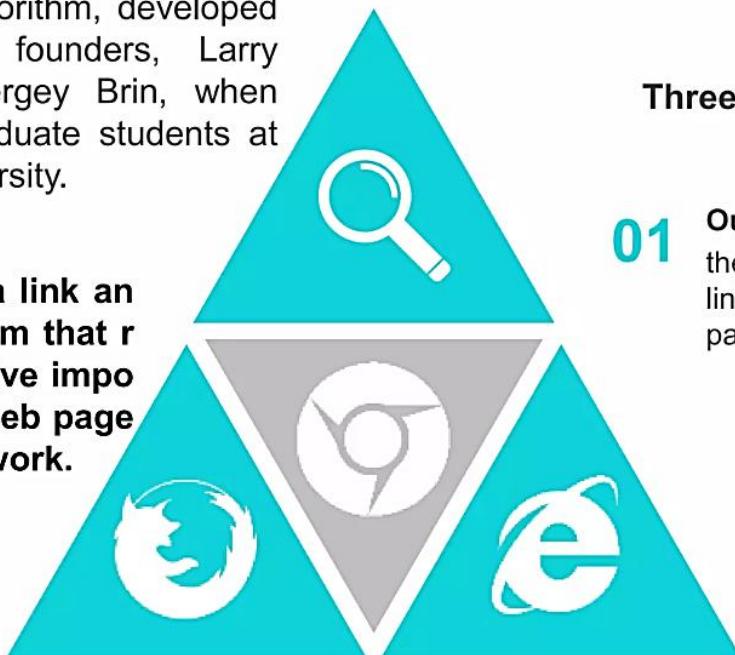
Big part of the MAGIC behind Google success is its PageRank Algorithm.

PageRank Algorithm



PageRank Algorithm, developed by Google's founders, Larry Page and Sergey Brin, when they were graduate students at Stanford University.

PageRank is a link analysis algorithm that ranks the relative importance of all web pages within a network.



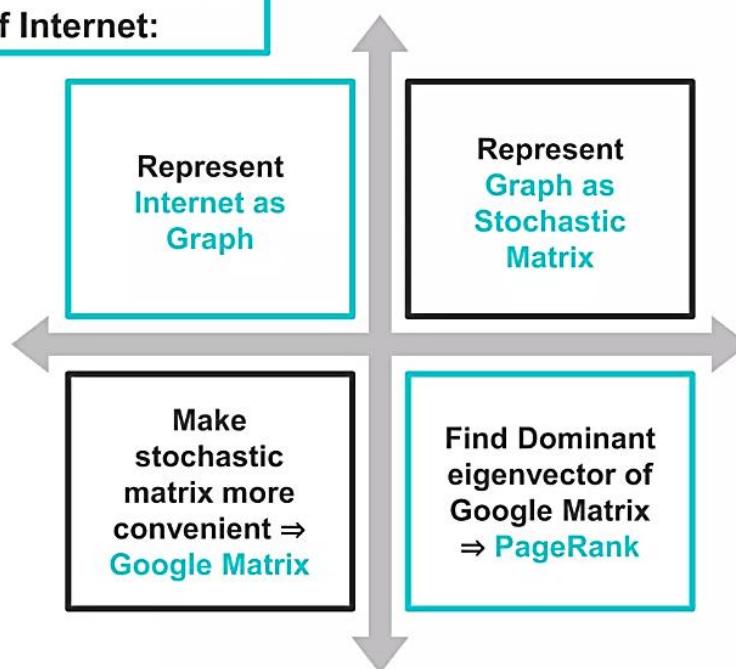
Three features for determining PageRank :

- 01 Outgoing Links**
the number of links found in a page
- 02 Incoming Links -**
the number of times other pages have cited this page
- 03 Rank**
A value representing the page's relative importance in the network.

PageRank – How it Works ?

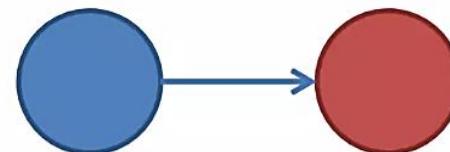


Mathematical Model
of Internet:



Internet as a Graph

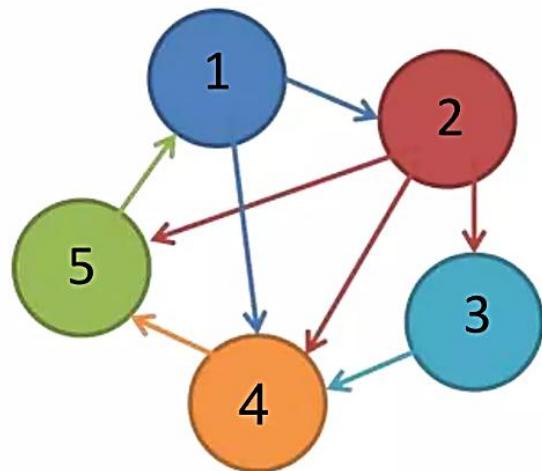
Link from one web page to another web page.



Web graph : Web pages = nodes, Links = edges

Continued...

Web graph as a Matrix



$$S = \begin{pmatrix} 0 & 1/2 & 0 & 1/2 & 0 \\ 0 & 0 & 1/3 & 1/3 & 1/3 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{pmatrix}$$

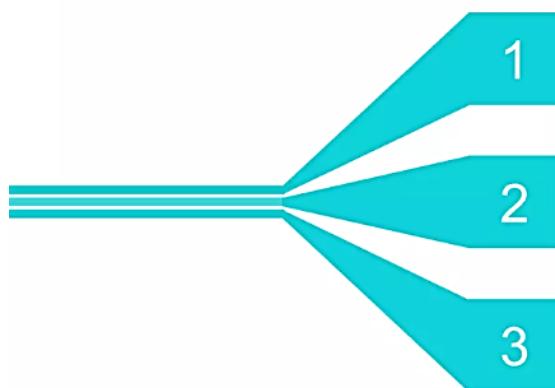
Links = nonzero elements in matrix

Every page 'i' has $l_i \geq 1$ outlinks. $S_{ij} = \begin{cases} 1/l_i & \text{if page } i \text{ has link to page } j \\ 0 & \text{otherwise} \end{cases}$

S is a Sparse Matrix, as most of the entries are zero.

Probability that surfer moves from page i to page j .

Importance of Linear Algebra



- 1 Using techniques of Linear Algebra, one can compute a unique solution for PageRank Problem.
- 2 It gives importance of all webpages in terms of PageRank Eigenvector corresponding to each webpage.
- 3 No other successful technique other than Linear Algebra is available to solve this problem.

Algorithms

- Introduction to Algorithms and Pseudo Code
- Searching Algorithms
- Sorting Algorithms
- Optimization Algorithms
- Recursive Algorithms
- Big-O Notation



Algorithms, coding theory, data structures

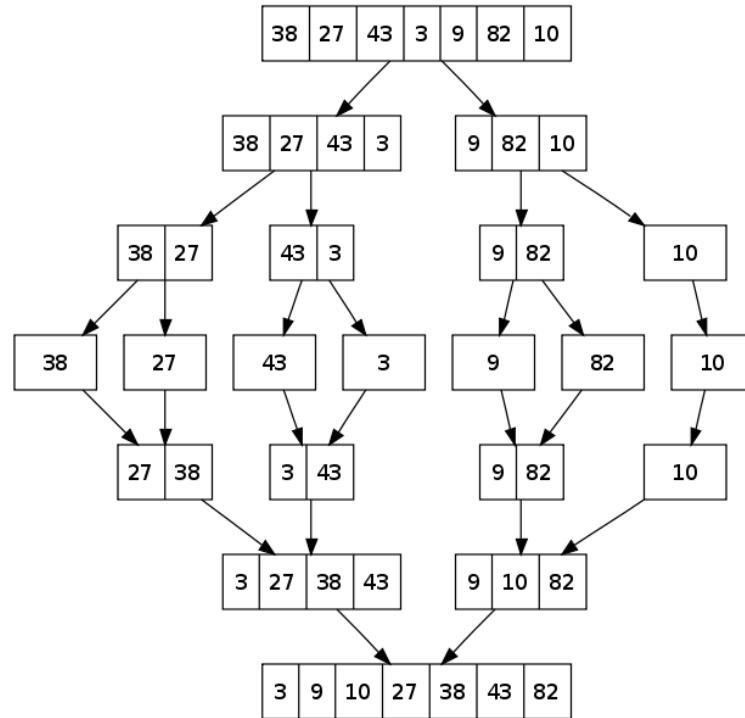
How many steps are needed to sort n numbers?

Algorithm 1 (Bubble Sort):

Every iteration moves the i -th smallest number to the i -th position

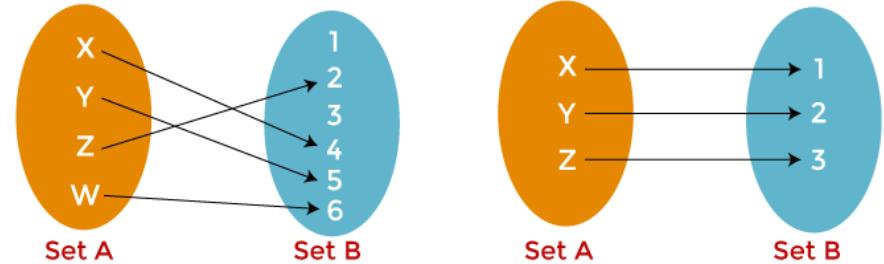
Algorithm 2 (Merge Sort):

Which algorithm runs faster?



Number Theory

- Cartesian Products and Ordered Pairs
- Relations



Database, algorithms, data structures

: Logic and Proofs

How do computers think?

Logic: propositional logic

Truth Tables

Conditionals and Negation

Proofs: direct, by case, induction, contradiction

$$\frac{x_1 + x_2 + \dots + x_n}{n} \geq \sqrt[n]{x_1 \cdot x_2 \cdots x_n}$$

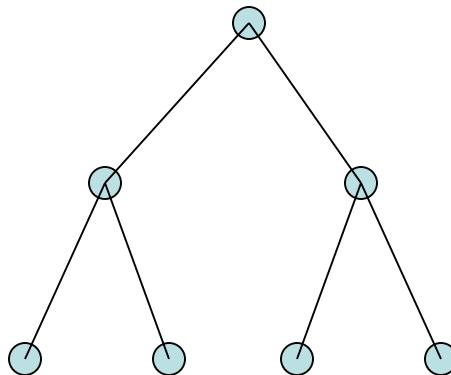
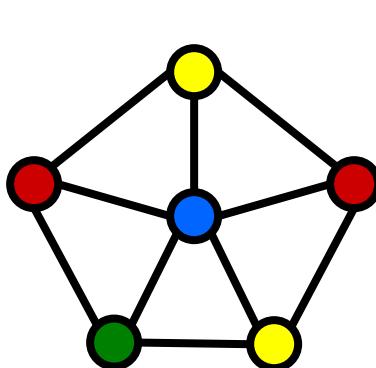
1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	

1	2	3	4
5	6	7	8
9	10	11	12
13	15	14	

Artificial intelligence, database, circuit, algorithms

Graph Theory

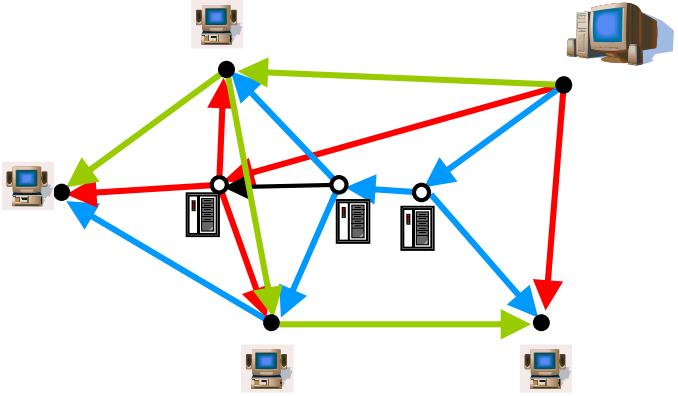
- Graphs
- Applications of Graphs
- Trees
- Dijkstra's Algorithm



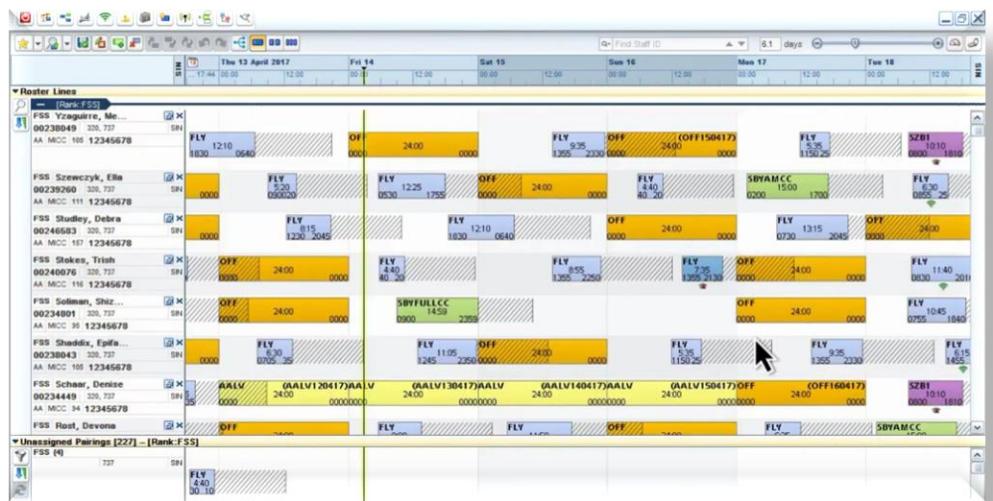
Computer networks, circuit design, data structures

Graph Theory

How to color a map?



How to send data efficiently?

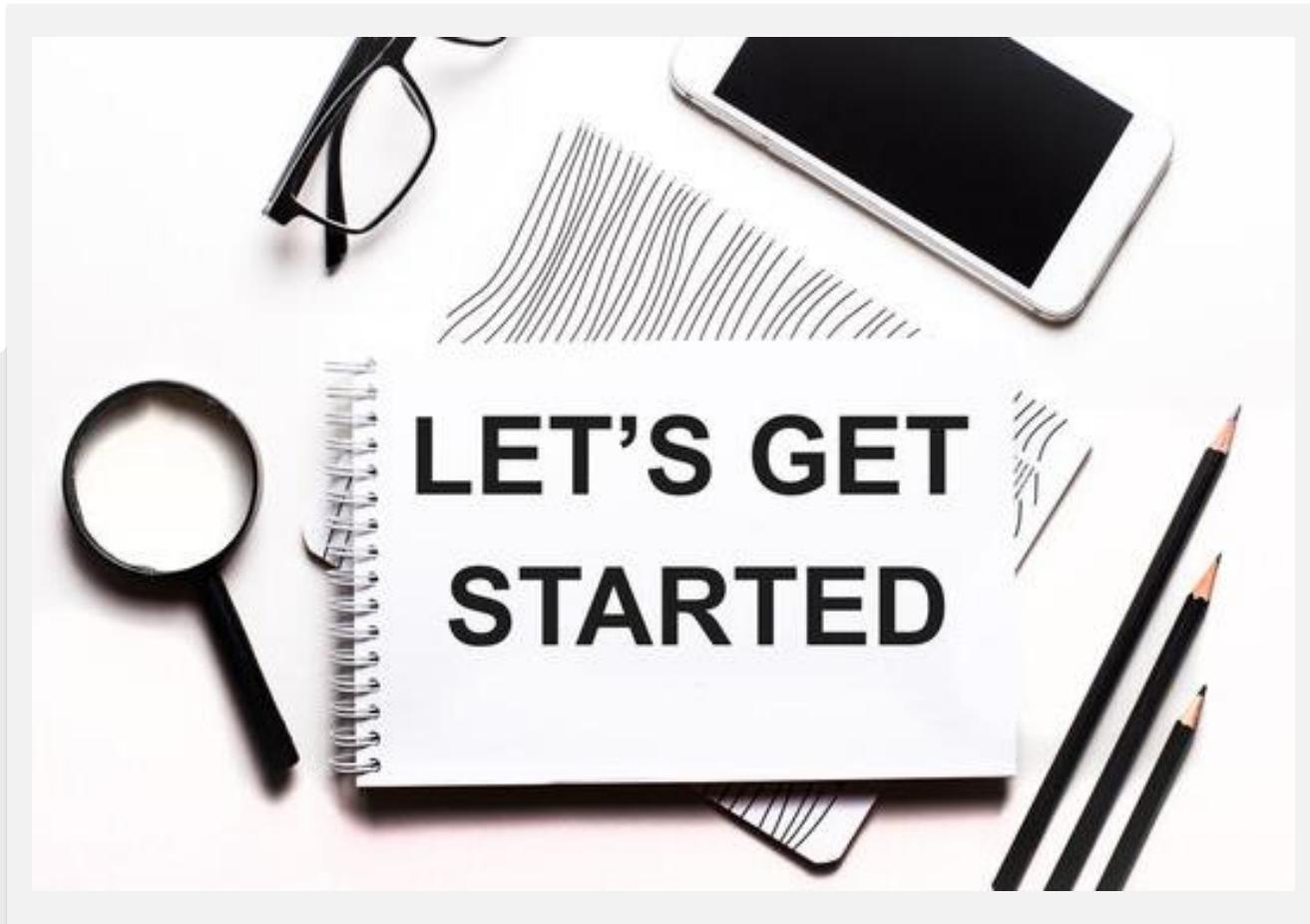


Crew Scheduling

Objectives of This Course

- ✓ To learn mathematical concepts that are related to Computer Science
- ✓ To be familiar with formal mathematical reasoning, e.g. logic, proofs
- ✓ To improve problem solving skills
- ✓ To see the connections between discrete mathematics and computer science





Thank you for your attention.

Course Books' Links

- chrome-extension://efaidnbmnnibpcajpcglclefindmkaj/http://www.toomey.org/tutor/text_books/Digital_Logic/Discrete%20Mathematics%20with%20Applications%20-%20Susanna%20S.%20Epp%20(2019).pdf
- chrome-extension://efaidnbmnnibpcajpcglclefindmkaj/https://readyforai.com/download/discrete-mathematics-and-its-applications-8th-edition-pdf/?wpdmld=1676&_wpdmkey=651a85506a31c
- chrome-extension://efaidnbmnnibpcajpcglclefindmkaj/https://faculty.ksu.edu.sa/sites/default/files/rosen_discrete_mathematics_and_its_applications_7th_edition.pdf